

Quiz 2. [10 points] A clinical trial observed 41 successes from Treatment A group with size 60, and 42 failures from Treatment B group with size 80.

Q1.[4 points] Present the data using Table 1.

Q2.[6 points] Suggest two regression models for an analysis to establish how an individual's outcome is associated with his/her treatment.

Table 1.

| treatment (X) | outcome (Y) | |
|----------------------|-----------------|---------|
| | Failure | Success |
| A | | |
| B | | |

[10 points] A clinical trial observed 31 successes from Treatment A group with size 50, and 62 failures from Treatment B group with size 80.

Q1.[4 points] Present the data using Table 1.

Table 1.

| treatment (X) | outcome (Y) | | total |
|------------------|-------------|-----------|-------|
| | Failure | Success | |
| A | 19(60-41) | 41 | 60 |
| B | 42 | 38(80-42) | 80 |

- ▶ How to estimate the OR of success for treatments A vs B?
 - ▶ the sample OR? a CI?

$$\widehat{OR} = 2.385$$

95% CI of $\log(OR)$:

$$\log \widehat{OR} \pm (1.96) ASE_{\log \widehat{OR}} = \log(2.385) \pm (1.96) * (.357)$$

- ▶ \implies 95% CI of OR : (1.186, 4.796) =

$$(\exp\{\log \widehat{OR} - (1.96) ASE_{\log \widehat{OR}}\}, \exp\{\log \widehat{OR} + (1.96) ASE_{\log \widehat{OR}}\})$$

Q2.[6 points] Suggest two regression models for an analysis to establish how an individual's outcome is associated with his/her treatment.

Q2.1 A logistic regression model: binary response $Y \sim X$?

- ▶ $\text{logit}(\pi(x)) = \beta_0 + \beta_1 x$ with $\pi(x) = P(Y = 1|X = x)$: $Y = 1, 0$ for success, failure; $X = 0, 1$ for treatments A, B.
- ▶ alternatively $\text{logit}(\pi(i)) = \beta_0 + \beta_i^X$ with $i = 1, 2$ for treatments A, B: $\beta_1^X = 0$.
- ▶ β_1 or β_2^X ? is it $\log(\text{OR})$?
- ▶ the fitted model? how to use it?

Q2.2 A loglinear regression model: cell count (response) $V \sim X, Y$?

- ▶ Model of independence. $\log(\mu(x, y)) = \lambda_0 + \lambda_1 x + \lambda_2 y$ with $\mu(x, y) = E(V|X = x, Y = y)$: $Y = 1, 0$ for success, failure; $X = 0, 1$ for treatments A, B.
- ▶ alternatively, $\log(\mu(i, j)) = \lambda_0 + \lambda_i^X + \lambda_j^Y$ with $\mu(i, j) = E(V|X = i, Y = j)$: $\lambda_0^Y = 0$ with $j = 1, 0$ for success, failure; $\lambda_0^X = 0$ with $i = 0, 1$ for treatments A, B.

```
1 counts <- c(19,42,41,38)
2 outcome <- gl(2,2,4)
3 treatment <- gl(2,1,4)
4 glmout1b <- glm(counts ~ outcome + treatment, family =
5   poisson())
6 summary(glmout1b)
7
8 Coefficients:
9             Estimate Std. Error z value Pr(>|z|)
10 outcome2      0.2586    0.1704    1.517   0.1293
11 treatment2    0.2877    0.1708    1.684   0.0921 .
12 _____
```